

Derivation of Gas Equation! —

From kinetic theory,

$$p = \frac{1}{3} \rho c^2$$

$$p = \frac{1}{3} \frac{M}{V} c^2$$

$$pV = \frac{1}{3} Mc^2$$

Let us consider one gram molecule of a gas at an absolute temperature T . The mean energy of the molecules

$$= \frac{1}{2} mc^2$$

$$= \frac{1}{2} Nm c^2$$

$$\therefore pV = \frac{1}{3} Nm c^2$$

$$= \frac{2}{3} N \cdot \frac{1}{2} mc^2$$

Mean kinetic energy of a molecule

$$= \frac{1}{2} m \bar{c}^2$$

$$= \frac{3}{2} kT$$

$$\therefore PV = \frac{2}{3} N \cdot \frac{3}{2} kT$$

$$PV = NkT$$

But

$$N \times k = R$$

$$\therefore PV = RT$$

This equation is called perfect gas equation

In this gas equation,

$$PV = RT$$

P is in dyne/cm²

R = 8.31×10^7 erg/gm mol-k

T is in K

V = the volume in cc per gram molecule.